Combining AHP and DEA Methods for Selecting a Project Manager

A project manager has a major influence on the success or failure of the project. A good project manager can match between the strategy and objectives of the organization and the goals of the project. Therefore, the selection of the appropriate project manager is a key factor for the success of the project. A potential project manager is judged by his or her proven performance and personal qualifications. This paper proposes a method to calculate the weighted scores and the full rank of candidates for managing a project, and to select the best of those candidates. The proposed method combines specific methodologies: the Data Envelopment Analysis (DEA) and the Analytical Hierarchical Process (AHP) and uses DEA Ranking Methods to enhance selection.

Keywords: Project Management (PM), Data Envelopment Analysis (DEA), Analytical Hierarchical Process (AHP), Ranking Methods (RM).

1. Introduction

The success of a project depends on several critical success factors. One important factor is supervision by a competent project manager with proven leadership skills (Fortune & White, 2006). In the selection process for a new project manager, his or her past performance should be considered, as should his or her personal and professional skills. If there are several candidates to manage an important project, it is common practice to select the best candidate on the basis of several criteria. The proposed method combines specific methodologies: the Data Envelopment Analysis (DEA) and the Analytical Hierarchical Process (AHP) and uses DEA Ranking Methods to enhance selection.

In selecting a project manager for a specific project his or her certification degree can be taken into account. It is common to assume that a project manager with a high level of certification is more competent than an uncertified project manager. There are several international associations that propose certification programs for project managers. For example, the project management institute (PMI) offers a certification program for
project practitioners of all education and skill levels. There are currently six credentials available (PMI, 2014). Another example is the international project management association (IPMA) that developed a 4-level system for project managers certification (IPMA, 2014). Level A is Certified Projects Director – one that manages complex project portfolios and programs. Level B is Certified Senior Project Manager – one that manages complex projects with a minimum of five years of experience. Level C is Certified Project Manager – one that manages projects of moderate complexity with a minimum of three years of experience. Level D is Certified Project Management Associate – one that applies project management knowledge when working on projects.

This paper is an expansion of the decision-making support system (DMSS) that was proposed by Hadad et al., (2013). The DMSS of Hadad et al., (2013) used only objective criteria in order to rank a group of candidates. This paper proposes to use the scores that each project obtains by the previous DMSS, as an input to a revised DMSS, and to use those results in combination with other qualitative and subjective criteria to obtain a full rank of the candidates.

The revised DMSS combines two well-known methodologies: Data Envelopment Analysis (DEA) (Charnes et al., 1978) and the Analytical Hierarchical Process (AHP) (Saaty, 1980). Moreover, the DMSS uses a ranking method in the context of the DEA (see Adler et al., 2002, Hadad & Hanani, 2011). Combining the AHP with the DEA can be found for example in: Sinuany-Stern et al., (2000); Hadad & Hanani (2011); Hadad et al., (2013); Yang & Kuo (2003), and others.

The paper is structured as follows: in section 2, a literature review and basic models are presented. Section 3 details the candidates ranking; in section 4 a real-life case study is described, and the final part of the paper is a summary.

2. Literature review

This section introduces the two well-known methodologies that are at the basis of the proposed model, the Data Envelopment Analysis (DEA) and the Analytical Hierarchical Process (AHP). The DEA evaluates the relative efficiency of Decision-Making Units (DMUs) and the AHP converts qualitative evaluations into quantitative criteria. Furthermore, this section introduces ranking methods in the DEA context that can be used to rank the project managers.

2.1 Data Envelopment Analysis (DEA)

The DEA (CCR model) was first developed by Charnes et al., (1978). The DEA is a non-parametric method that uses multiple inputs and outputs to evaluate the relative efficiency of DMUs. It is a tool that is widely used in the private and public sectors, and provides a mechanism for measuring an identified DMU efficiency (in our case, the project), compared with other DMUs. Surveys of DEA applications can be found in Seiford (1996) and in Emrouznejad et al., (2008). There are also many papers that use the DEA for comparing project efficiency (for example, Vitner et al., 2006; Eilat et al., 2006; Mahmood et al., 1996, Hadad et al., 2013, and Hadad & Keren, 2013).

The DEA measures the relative efficiency score as a ratio between weighted output and weighted input. The DEA calculates for each DMU k the ideal weights for each output: \( U_r^k \) \((r = 1, 2, \ldots, s)\), and the ideal weights for each input: \( V_i^k \) \((i = 1, 2, \ldots, m)\), thereby maximizing its relative efficiency score under the restriction that this score is bound by 100% efficiency. The weights vary from DMU to DMU. If a DMU with its ideal weights receives an efficiency score of 100%, it is efficient, while a score of less than 100% is considered inefficient.

Consider \( n \) projects, where each project \( j \) \((j = 1, \ldots, n)\) is characterized by \( m \) input types \( \tilde{X}_j = (X_{1j}, X_{2j}, \ldots, X_{mj})^T > 0 \) and by \( s \) output types \( \tilde{Y}_j = (Y_{1j}, Y_{2j}, \ldots, Y_{sj})^T > 0 \). The CCR model (output-maximized) for project \( k \) is formulated as follows:
The CCR model assumes that the production function exhibits Constant Returns To Scale (CRTS). The results of the CCR output-maximized formulation are identical to the CCR input-minimized results (Adler et al., 2002).

2.2 Analytical Hierarchical Process

The Analytical Hierarchical Process (AHP) methodology was developed by Saaty (1980). The AHP methodology is used to quantify the value of qualitative or subjective criteria. The AHP has been widely used in real-life applications (see a survey in Zahedi 1986, Vaidya & Kumar 2006, Hadad & Hanani, 2011). In our case each project manager is evaluated according to several criteria, not all of them quantitative. The output of the AHP is shown by numeric scores of each project manager in each qualitative or subjective criterion. The input of the AHP is a pairwise comparison matrix for every pair of project managers, for each qualitative or subjective criterion that is created by the decision makers. A common scale of values for pairwise comparison ranges from 1 (indifference) to 9 (extreme preference). The pairwise comparison matrix has an element \( a_{ij} \), and each element in the matrix is strictly positive. For \( n \) project managers and \( m \) criteria, the number of comparisons to be carried out is \( m(n^2 - n) / 2 + m(m-1)/2 \). According to Saaty’s definition, the eigenvector \( \vec{\lambda} \), of the maximal eigenvalue \( \hat{\lambda}_{\text{max}} \) of each pairwise comparison matrix, is utilized for ranking the project managers. For more detail about AHP methodology see Saaty (1980, 1986, 1990). The AHP has been widely used in real-life applications (see a survey in Hadad & Hanani, 2011).

Saaty (1980) defined a statistical measure to test the consistency of the respondent. The statistical measure of the consistency index (CI) is:

\[
CI = \mu = \frac{\hat{\lambda}_{\text{max}} - n}{n - 1}
\]

and the Consistency Ratio (CR) is given by:

\[
CR = \left( \frac{CI}{RI} \right) \times 100\%
\]

Where \( \varepsilon \) is an infinitesimal number.

\[
h_k = \max_{r=1}^{s} \sum_{r=1}^{s} U^k_r \times Y_{rk}
\]

subject to

\[
\sum_{r=1}^{m} V^k_i \times X_{rk} = 1
\]

\[
\sum_{r=1}^{s} U^k_r \times Y_{fi} - \sum_{i=1}^{m} V^k_i \times X_{ij} \leq 0 \quad j = 1, \ldots, n
\]

\[
U^k_r \geq \varepsilon > 0 \quad r = 1, 2, \ldots, s
\]

\[
V^k_i \geq \varepsilon > 0 \quad i = 1, 2, \ldots, m
\]
where:
\( \lambda_{\text{max}} \) - is the maximal eigenvalue of the matrix,
\( n \) - is the number of rows/columns of the matrix,
\( RI \) - is the random index. It is the average of the CI for a large number of randomly generated matrices.

The values of \( RI \) can be found in the table developed by Saaty (1980, p.51).

The consistency of the decision makers can be checked by the value of \( CR \). Generally, if the \( CR \) is 10% or less, the respondent is considered consistent and acceptable, and the computed comparison matrix can be used (Saaty, 1980). If the \( CR \) is higher than 10%, the respondent is not consistent and his or her pairwise estimations must be corrected.

2.3 Ranking methods

There are many different methods for ranking DMUs within the DEA context (for reviews see Adler et al., 2002, Hadad & Hanani, 2011). The following sub-section presents two of them.

2.3.1 The Super Efficiency method

One drawback of the DEA methodology is that it does not rank efficient DMUs (those with efficiency scores of 1). To overcome this drawback Anderson & Peterson (1993) proposed the Super efficiency ranking method. They suggest allowing the efficient DMUs to receive a score higher than 1 by dropping the constraint that bounds the score of the evaluated efficient DMU to 1. The Anderson & Peterson formulation for the DMU is follows:

\[
 h_k = \text{Max} \sum_{r=1}^{s} U_r^k \times Y_{rk} \\
 s.t. \\
 \sum_{r=1}^{s} U_r^k \times Y_{rf} = \sum_{i=1}^{m} V_i^k \times X_{ij} \leq 0 \quad \text{for } j = 1, 2, \ldots, n, j \neq k \\
 \sum_{i=1}^{m} V_i^k \times X_{ik} = 1 \\
 U_r^k \geq \varepsilon > 0 \quad r = 1, 2, \ldots, s \\
 V_i^k \geq \varepsilon > 0 \quad i = 1, 2, \ldots, m
\]

2.3.2 The Cross Efficiency method

Another drawback of DEA methodology is that it does not use common weights while evaluating the efficiency of DMUs. To overcome this drawback Sexton et al., (1986) proposed the Cross Efficiency (CE) ranking method. This subsection presents the steps in using the CE to set the score of each DMU.

Step 1 – Find the optimal weights \( u_r^k \) \((r = 1, 2, \ldots, s; k = 1, 2, \ldots, n)\) and \( v_i^k \) \((i = 1, 2, \ldots, m; k = 1, 2, \ldots, n)\) by the CCR model.
Step 2 – Calculate the elements of the cross-evaluation matrix as follows:

\[
h_{k,j} = \frac{\sum_{r=1}^{S} u_r^k \times Y_{r,j}}{\sum_{i=1}^{m} v_i^k \times X_{r,j}}, \quad k = 1, 2, ..., n, \quad j = 1, 2, ..., n
\]

Thus, \( h_{k,j} \) represents the efficiency given to DMU \( j \) in the CCR run of DMU \( k \) (the efficiency of DMU \( j \) by the optimal weights of DMU \( k \)).

Step 3 – Calculate the score for each DMU \( j \) as follows:

\[
\bar{h}_j = \frac{\sum_{j=1}^{n} h_{k,j}}{n}
\]

Step 4 – Rank the DMUs according to the scores \( \bar{h}_j \), \( j = 1, 2, ..., n \). The DMU with the highest score will be ranked first, and so on.

2.4 Inputs and outputs for ranking projects

Many quantitative criteria can be used to compare the relative performance of completed projects. The decision makers must determine the appropriate criteria for project evaluation and how those criteria can be measured, bearing in mind that they should reflect the organization’s objectives and the project types. In order to use the ranking method in the DEA context, the criteria must be classified into inputs and outputs. Hadad et al., (2013) proposed the following inputs and outputs:

**Input 1** - The cost stabilization coefficient of project \( i \).

\[
X_{1,i} = \frac{E(C_i)}{\sigma(C_i)}
\]

where
- \( E(C_i) \), the expected cost of the \( i \)-th project.
- \( \sigma(C_i) \), the standard deviation cost of the \( i \)-th project.
- \( X_{1,i} \), the coefficient of variation (Levy & Sarnat, 1995).

**Input 2** - The completion time stabilization coefficient of project \( i \).

\[
X_{2,i} = \frac{E(T_i)}{\sigma(T_i)}
\]

**Input 3** - The reciprocal of the intensity of project \( i \).

\[
X_{3,i} = \frac{E(T_i)}{E(C_i)}
\]
Output 1 - The ratio between the expected cost and the actual cost of project $i$.

\[ Y_{1,i} = \frac{E(C_i)}{e(C_i)} \]  

(7)

Where $e(C_i)$ represents the implementation expenses of the $i$-th project.

Output 2 - The ratio between the expected and the actual completion time of project $i$.

\[ Y_{2,i} = \frac{E(T_i)}{e(T_i)} \]  

(8)

Output 3 - The ratio between the actual cost, excluding implementation expenses, and the implementation expenses of project $i$.

\[ Y_{3,i} = \frac{e(C_i)}{I(C_i)} \]  

(9)

Where $I(C_i)$ represents the implementation expenses of the $i$-th project.

Output 4 - The ratio between the actual completion time, excluding the implementation duration, and the implementation duration of project $i$.

\[ Y_{4,i} = \frac{e(T_i)}{I(T_i)} \]  

(10)

3. Candidate ranking

This section presents the steps of the proposed method that enables a full ranking of the candidates. The ranking is carried out according to the average scores of the projects that each project manager performed in the past, and according to the scores of his or her personal qualitative criteria.

Step 1: Define the candidates to be evaluated. For each candidate $k$, $k = 1, 2, ..., K$, determine the projects that will be used for candidate ranking $l = 1, 2, ..., L_k$. $L_k$ is the number of projects according to which the candidate $k$ will be evaluated.

Step 2: Calculate for each project $k, l$ the input and output values according to equations (4), (7), (8), (9), respectively.

Step 3: Select one of the ranking methods (section 2.3) and compute the level of performance, $F_{k,l}$, for all the projects $k, l$, $k = 1, 2, ..., K$; $l = 1, 2, ..., L_k$. For the Anderson & Peterson ranking method use equation (2) to compute $F_{k,l}$. For the CE ranking method use equation (2) to calculate the optimum weights and then use equation (3) to compute $F_{k,l}$.

Step 4: The average level of past performance of candidate $k$ is calculated as follows:

\[ F_k = \frac{1}{L_k} \sum_{l=1}^{L_k} F_{k,l} \]  

(11)
Step 5: Determine the qualitative personal criteria according to which the candidates will be evaluated. For each criterion \( t, t = 1,2,\ldots,T \) perform pairwise comparisons according to AHP methodology and create a pairwise comparison matrix \( A_{t} \). Calculate for these matrices \( \lambda_{t,max} \) and the consistency ratio \( CR_{t} \). If \( CR_{t} \leq 10\% \), go to the next step. If not, the pairwise comparison must be modified.

Step 6: Calculate the normalized eigenvector \( \tilde{N}_{t} \ (t = 1,2,\ldots,T) \) of the maximum eigenvalue \( \lambda_{t,max} \). The elements of this vector, \( P_{k,t} \), represent the score of candidate \( k \) in criterion \( t \).

Step 7: Determine the relative weights, \( W_{t} \ (t = 1,2,\ldots,T,T+1) \) for all the criteria (qualitative and quantitative). Note that there are \( T \) criteria that represent the qualitative attributes of the candidate and one quantitative criterion that represents his or her past performance level. The relative weights can be set directly by the decision makers, either subjectively by the AHP, or objectively by the DEA.

Step 8: The final score of each candidate, \( S_{k} \), is the weighted score he or she obtained for all the criteria. This score is calculated as follows:

\[
S_{k} = \sum_{t=1}^{T} W_{t} \times P_{k,t} + W_{T+1} \times F_{k} 
\]  

(12)

Step 9: Rank all the candidates by \( S_{k} \). The candidate with the highest \( S_{k} \) is ranked first, and so on.

4. The case study

This section presents a real-life case study that demonstrates the applicability of the proposed method. The raw data of the level of performance are taken from Hadad et al., (2013). In this case study there are 11 candidates (A,B,…,K) that together performed 52 projects in the past as illustrated in Table 1. Hadad et al., (2013) calculated the score of each of the 52 projects by the CE ranking method. Here the performance level for each project manager is calculated as the average scores of the CE data of his or her projects. The performance score is normalized in order to obtain a sum of the scores that will equal 1. The results are given in Table 1.

<table>
<thead>
<tr>
<th></th>
<th>Performance</th>
<th>No. of projects</th>
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<tbody>
<tr>
<td>A</td>
<td>0.0852</td>
<td>4</td>
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<tr>
<td>B</td>
<td>0.0852</td>
<td>5</td>
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<tr>
<td>C</td>
<td>0.0848</td>
<td>5</td>
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<tr>
<td>D</td>
<td>0.1027</td>
<td>7</td>
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<td>E</td>
<td>0.0851</td>
<td>3</td>
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<tr>
<td>F</td>
<td>0.1065</td>
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<td>G</td>
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<td>H</td>
<td>0.0856</td>
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<td>J</td>
<td>0.0890</td>
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<tr>
<td>K</td>
<td>0.0895</td>
<td>5</td>
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<tr>
<td>Sum</td>
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<td>52</td>
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</table>
Beyond the level of performance, the decision maker decided to take into account three qualitative criteria: leadership, technical skills and the level of certification in order to improve the ranking of the candidates. Here are the pairwise matrices (Table 2 and Table 3) for the qualitative criteria.

**Table 2**: The pairwise matrix for leadership

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For the leadership criterion \( \lambda_{\text{max}} = 12.4205 \). The consistency measure of the respondent is:

\[
CI = \mu = \frac{\lambda_{\text{max}} - n}{n - 1} = \frac{12.4205 - 11}{11 - 1} = 0.1421
\]

\[
CR = \left( \frac{CI}{RI} \right) 100\% = \left( \frac{0.1421}{1.51} \right) 100\% = 9.4\% < 10\%
\]

Hence, the respondent can be considered consistent, and the comparison matrix can be used. The leadership score of each project manager is calculated by the following normalized eigenvector:

\[
\hat{N}_1 = \left\{ 0.1397, 0.0545, 0.0299, 0.0261, 0.0165, 0.2496, 0.1309, 0.0674, 0.0684, 0.1628, 0.0541 \right\}
\]

**Table 3**: The pairwise matrix for technical skills

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</tr>
<tr>
<td>J</td>
<td>1</td>
<td>3</td>
<td>3</td>
<td>1</td>
<td>3</td>
<td>3</td>
<td>3</td>
<td>3</td>
<td>1/3</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>K</td>
<td>3</td>
<td>9</td>
<td>9</td>
<td>3</td>
<td>9</td>
<td>9</td>
<td>9</td>
<td>3</td>
<td>1/3</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

For the technical skills criterion \( \lambda_{\text{max}} = 12.1603 \). The consistency measure of the respondent is:

\[
CI = \mu = \frac{\lambda_{\text{max}} - n}{n - 1} = \frac{12.1603 - 11}{11 - 1} = 0.1160
\]

\[
CR = \left( \frac{CI}{RI} \right) 100\% = \left( \frac{0.1160}{1.51} \right) 100\% = 7.7\% < 10\%
\]
Hence, the respondent can be considered consistent, and the comparison matrix can be used. The technical skills and the score of each project manager are calculated by the following normalized eigenvector:

\[ \tilde{N}^T = \{0.0760,0.0283,0.0180,0.0820,0.0283,0.0426,0.0230,0.0573,0.3425,0.1107,0.1912\} \]

In general, the candidates may have official certifications from different national or international associations, and different levels of certification (for example, level A or level D of IMPA certification). In our case the candidates were classified into three groups: the first group includes candidates without certification (score 1), the second group includes candidates with basic certification (score 2), and the third group includes candidates with expert certification (score 3) in project management. The scores of the certification levels were normalized and presented in Table 4. Table 4 summarizes the normalized scores of leadership, technical skills, performance level and certification level for each project manager.

### Table 4: The normalized scores of each project manager

<table>
<thead>
<tr>
<th>manager</th>
<th>leadership</th>
<th>technical skills</th>
<th>performance</th>
<th>certification</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.1397</td>
<td>0.0760</td>
<td>0.0852</td>
<td>0.05</td>
</tr>
<tr>
<td>B</td>
<td>0.0545</td>
<td>0.0283</td>
<td>0.0852</td>
<td>0.05</td>
</tr>
<tr>
<td>C</td>
<td>0.0299</td>
<td>0.0180</td>
<td>0.0848</td>
<td>0.10</td>
</tr>
<tr>
<td>D</td>
<td>0.0261</td>
<td>0.0820</td>
<td>0.1027</td>
<td>0.05</td>
</tr>
<tr>
<td>E</td>
<td>0.0165</td>
<td>0.0283</td>
<td>0.0851</td>
<td>0.10</td>
</tr>
<tr>
<td>F</td>
<td>0.2496</td>
<td>0.0426</td>
<td>0.1065</td>
<td>0.10</td>
</tr>
<tr>
<td>G</td>
<td>0.1309</td>
<td>0.0230</td>
<td>0.1060</td>
<td>0.15</td>
</tr>
<tr>
<td>H</td>
<td>0.0674</td>
<td>0.0573</td>
<td>0.0856</td>
<td>0.05</td>
</tr>
<tr>
<td>I</td>
<td>0.0684</td>
<td>0.3425</td>
<td>0.0864</td>
<td>0.10</td>
</tr>
<tr>
<td>J</td>
<td>0.1628</td>
<td>0.1107</td>
<td>0.0890</td>
<td>0.10</td>
</tr>
<tr>
<td>K</td>
<td>0.0541</td>
<td>0.1912</td>
<td>0.0835</td>
<td>0.15</td>
</tr>
</tbody>
</table>

In order to calculate the final score of each project manager the decision makers should determine the relative weights, \( w_t \) (\( t = 1,2,3,4 \)), for all the criteria. In our case these weights were determined by the AHP. Table 5 is the pairwise matrix for the three criteria as set by the decision makers.

### Table 5: The pairwise matrix for the criteria

<table>
<thead>
<tr>
<th></th>
<th>leadership</th>
<th>technical skills</th>
<th>performance</th>
<th>certification</th>
</tr>
</thead>
<tbody>
<tr>
<td>leadership</td>
<td>1</td>
<td>3</td>
<td>1/5</td>
<td>5</td>
</tr>
<tr>
<td>technical skills</td>
<td>1/3</td>
<td>1</td>
<td>1/7</td>
<td>7</td>
</tr>
<tr>
<td>performance</td>
<td>5</td>
<td>7</td>
<td>1</td>
<td>1/9</td>
</tr>
<tr>
<td>certification</td>
<td>1/5</td>
<td>1/7</td>
<td>9</td>
<td>1</td>
</tr>
</tbody>
</table>

In this matrix \( \lambda_{max} = 4.2685 \), and the consistency measure of the respondent is:

\[
CI = \mu = \frac{\lambda_{max} - n}{n-1} = \frac{4.2685 - 4}{4 - 1} = 0.0895
\]

\[
CR = \left(\frac{CI}{RI}\right) \times 100\% = \left(\frac{0.0895}{0.90}\right) \times 100\% = 9.94\% < 10\%
\]

Hence, the respondent can be considered consistent, and the comparison matrix is applicable. The weight of each criterion is calculated by the following normalized eigenvector:

\[ \tilde{N}^T = \{0.2189,0.1361,0.6013,0.0437\} \]
The final score of each candidate is the weighted score he or she obtained in all the criteria. The normalized final scores and the ranks of the candidates are presented in Table 6. One can see that F is the most suitable candidate to be selected as project manager.

Table 6: The final score and the rank of candidates

<table>
<thead>
<tr>
<th>manager</th>
<th>score</th>
<th>rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>I</td>
<td>0.9152</td>
<td>2</td>
</tr>
<tr>
<td>J</td>
<td>0.8428</td>
<td>3</td>
</tr>
<tr>
<td>G</td>
<td>0.7922</td>
<td>4</td>
</tr>
<tr>
<td>K</td>
<td>0.7345</td>
<td>5</td>
</tr>
<tr>
<td>A</td>
<td>0.7322</td>
<td>6</td>
</tr>
<tr>
<td>D</td>
<td>0.6272</td>
<td>7</td>
</tr>
<tr>
<td>H</td>
<td>0.5915</td>
<td>8</td>
</tr>
<tr>
<td>B</td>
<td>0.5371</td>
<td>9</td>
</tr>
<tr>
<td>C</td>
<td>0.4995</td>
<td>10</td>
</tr>
<tr>
<td>E</td>
<td>0.4890</td>
<td>11</td>
</tr>
</tbody>
</table>

Conclusion

This paper proposes a method that uses the DEA and AHP methodologies, together with the ranking method, for selecting the best candidate for managing a project. The proposed method allows calculating the weighted score and the rank of each candidate according to quantitative and qualitative criteria. It is important to select the appropriate criteria for the ranking because the selected criteria have influence on the final rank. The values of the criteria (quantitative and qualitative) are based on the past performance of the candidates. Therefore, this method is applicable only in case of experienced candidates. The proposed method can be used in project-oriented organizations such as building companies and software companies, where all projects have similar characteristics.

The limitation of the proposed model is that it is applicable only to experienced project managers and only in the cases where full data of past projects are available. Another limitation is that it needs subjective evaluations that must be carried out by decision makers. Decision makers are not always consistent \((CR > 10\%)\) and their evaluations may cause conflicts when several decision makers have different opinions.

REFERENCES:


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